

# Estimating uncertainty in remotely sensed soil moisture at continental to global scales

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with

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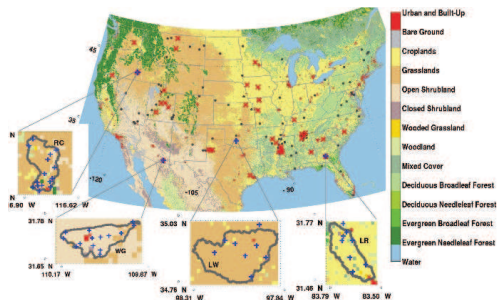
Vahid Naeimi and Wolfgang Wagner

Draper et al, 2013. (RSE)

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## Motivation/Outline (1)

- ▶ Aim: estimate large-scale distributed Root Mean Square Errors (RMSE) in remotely sensed near-surface soil moisture
  - ▶ For data assimilation observation error specification
  - ▶ For general evaluation (comparison to target accuracies for remotely sensed products)
- ▶ Difficulty: there is no agreed upon true soil moisture across continental scale domain



SCAN and ARS in situ sensors, from Liu et al (2011)

## Motivation/Outline (2)

- ▶ Demonstrate two methods for estimating distributed errors:
  - ▶ Triple collocation
  - ▶ Error propagation through remote sensing retrieval algorithms
- ▶ Apply to two remotely sensed soil moisture data sets:
  - ▶ AMSR-E X-band Land Parameter Retrieval Model (de Jeu and Owe, 2003)
  - ▶ ASCAT C-band TUWien empirical change detection (Wagner et al, 1999)
  - ▶ Jan. 2007 - Oct 2011, over a North American domain

## Rescaling of continental-scale soil moisture

- ▶ At large spatial scales, systematic differences between the mean and variance of different soil moisture estimates are ubiquitous, and the true mean and variance is unknown
- ▶ When comparing different soil moisture estimates, for evaluation or data assimilation:
  - ▶ It is standard to rescale all data sets to have mean and variance consistent with a chosen reference climatology
  - ▶ Focus is then on comparing their temporal changes

## Triple collocation ( $RMSE^{TC}$ )

- ▶ For ASCAT ( $\theta(A)$ ), AMSR-E LPRM ( $\theta(L)$ ), and Catchment model near-surface soil moisture ( $\theta(C)$ ) soil moisture anomalies from the mean seasonal cycle
- ▶ Assume an additive random error model ( $\langle \epsilon(X) \rangle = 0$ ):  
$$\theta(A) = \alpha(\theta + \epsilon(A))$$
$$\theta(L) = \lambda(\theta + \epsilon(L))$$
$$\theta(C) = \gamma(\theta + \epsilon(C))$$
- ▶  $\theta = \text{truth}$ , and  $\alpha, \lambda, \gamma$  are calibration constants
- ▶ Assume errors are not correlated with each other, or with the true state

Stoffelen (1998), Scipal et al (2008), Miralles et al (2010)

## Triple collocation ( $RMSE^{TC}$ )

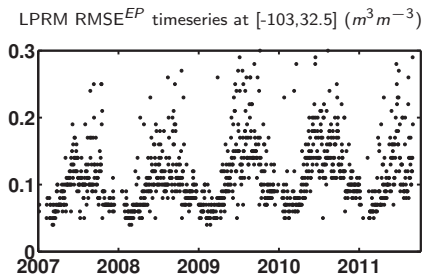
- ▶ Cannot solve for all three calibration constants and the errors, set  $\theta(A)$  as the reference data set ( $\alpha = 1$ )
- ▶ Solve for remaining calibration constants:  $\hat{\lambda}_A, \hat{\gamma}_A$
- ▶ Solve for  $\epsilon^2 = (RMSE^{TC})^2$ :  $\hat{\epsilon}_A^2(A), \hat{\epsilon}_A^2(L), \hat{\epsilon}_A^2(C)$

Note:

- ▶ Rescaling by variance results in biased  $RMSE^{TC}$ : must use triple collocation calibration
- ▶ Assumptions are violated if apply to original soil moisture time series: must use anomalies

## Error propagation ( $RMSE^{EP}$ )

- ▶ Propagate expected errors in input observations and parameters through the soil moisture retrieval model
  - ▶ ASCAT (Naeimi et al, 2007)
  - ▶ LPRM (Parinussa et al, 2011)



- ▶ Reported the average of the time series at each location

## Comparison of methods

Triple collocation :

- ▶ Estimates RMSE of the soil moisture anomalies, relative to the selected reference data set
- ▶ Can be used to compare errors in different data sets

Error Propagation:

- ▶ Estimates soil moisture errors due to errors in retrieval model parameters and input only (assumed to be RMSE of soil moisture anomalies)
- ▶ Input uncertainties are specified somewhat arbitrarily, hence magnitude of estimated RMSE is not informative
- ▶ Designed instead to detect (temporal/spatial) variation in errors

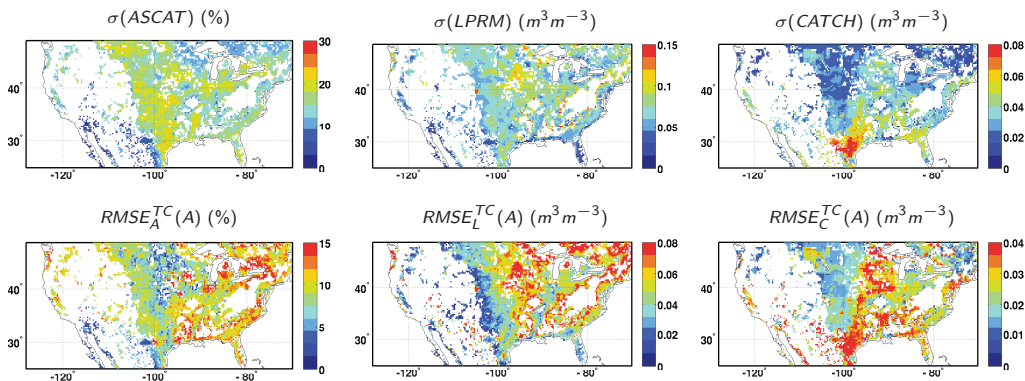


## Interpretation of soil moisture RMSE over large domains

## Soil moisture RMSE over large domains

- ▶  $\sqrt{\langle (X - Y)^2 \rangle} = \sqrt{\sigma(X)^2 + \sigma(Y)^2 - 2R\sigma(X)\sigma(Y) + b^2}$   
Because  $\sigma$  differs from place to place ... a single global RMSE target may not be appropriate.” (Entekhabi et al, 2010)
- ▶ For error estimates based on rescaled data sets:
  - ▶ RMSE depends on the reference  $\sigma$
  - ▶ Information on temporal agreement is from  $R$

## Dependence of RMSE on the reference



- Magnitude and spatial variability in RMSE strongly influenced by the reference  $\sigma$

## Fractional RMSE (*fRMSE*)

- ▶ Spatial differences in  $\sigma$  are not linear: the ratio (and ranking!) of the domain-average RMSE in  $m^3 m^{-3}$  depends on the selected reference

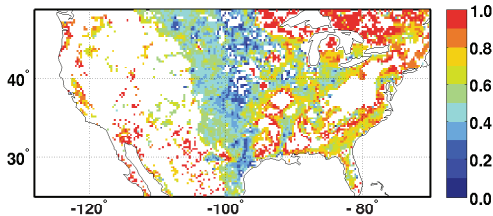
Reference	Mean $RMSE^{TC}$		
	A	L	C
ASCAT (%)	10	18	19
LPRM ( $m^3 m^{-3}$ )	0.07	0.06	0.09
CATCH ( $m^3 m^{-3}$ )	0.07	0.08	0.03

- ▶ RMSE is not well suited to continental scale soil moisture evaluation
- ▶ Here: report errors as  $fRMSE = RMSE_X(X)/\sigma(X)$   
(unitless, with range  $[0,1]$  )

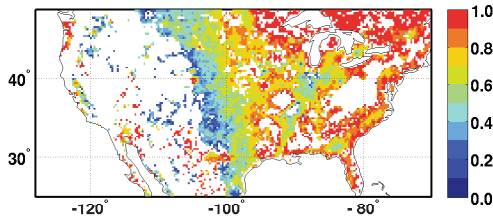
## Triple Collocation Results

# Triple collocation $fRMSE^{TC}$

ASCAT  $fRMSE^{TC}$

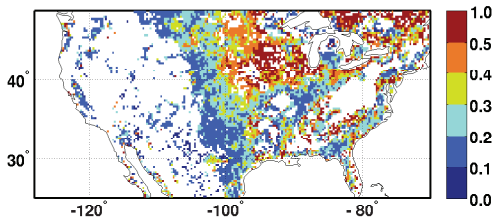


LPRM  $fRMSE^{TC}$

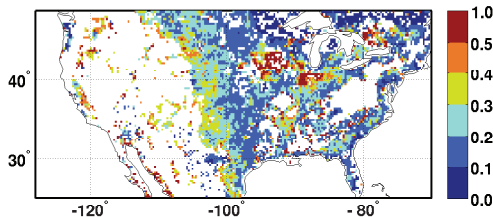


## ► $fRMSE^{TC}$ uncertainty (boot-strapped)

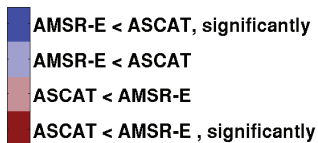
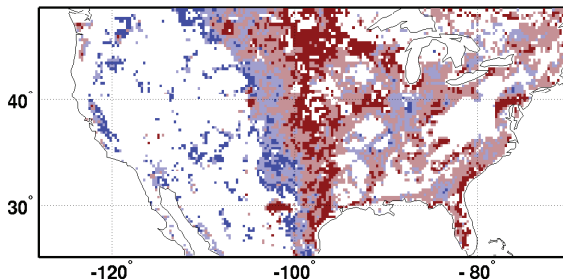
ASCAT  $fRMSE^{TC}$  90% C.I. (full width)



LPRM  $fRMSE^{TC}$  90% C.I. (full width)



## ASCAT and LPRM AMSR-E fRMSE<sup>TC</sup> comparison

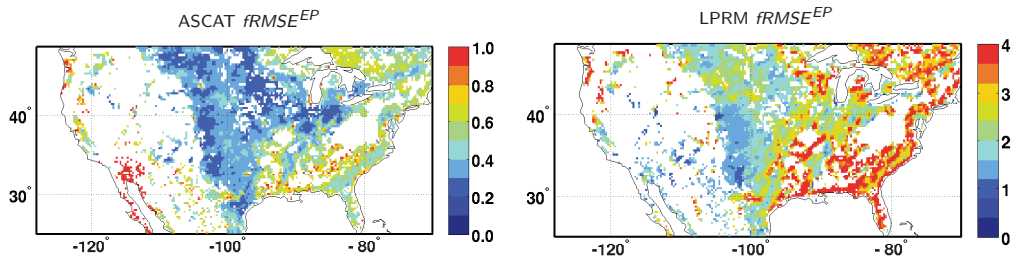


See also Crow and Zhan (2007), Scipal et al (2008), Dorigo et al (2010)

## Error propagation results

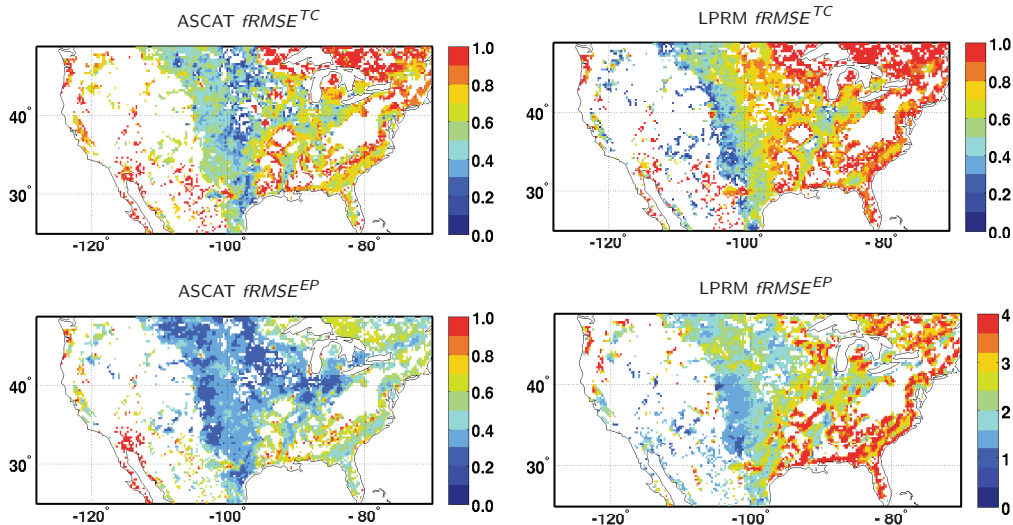


## Error propagation fRMSE ( $fRMSE^{EP}$ )

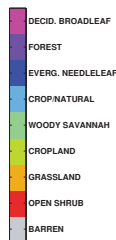
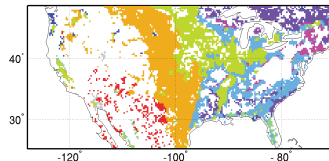
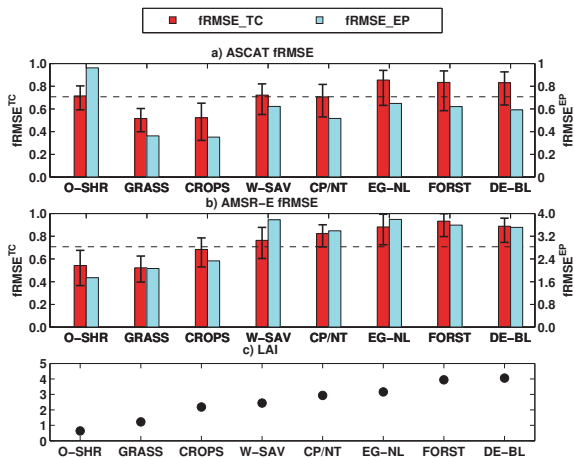


- ▶ Note: LPRM  $fRMSE^{EP}$  unphysically large

# fRMSE<sup>TC</sup> and fRMSE<sup>EP</sup> maps



# fRMSE<sup>TC</sup> and fRMSE<sup>EP</sup> by land cover



- ▶ ASCAT and AMSR-E fRMSE appear similar, although AMSR-E is more dependent on vegetation cover

## Conclusions (1/3)

How should we evaluate remotely sensed soil moisture globally?

- ▶ Substantial spatial variation in RMSE and fRMSE across North America
  - ▶ Evaluation based on handful of pixels may not represent global accuracy
  - ▶ Triple collocation or error propagation both provide useful uncertainty estimates that can complement comparison to in situ observations
- ▶ RMSE not a good choice of metric for large-scale evaluation
  - ▶ Uniform RMSE target over large domain not sensible
  - ▶ Selection of reference determines RMSE magnitude (domain-average RMSE has non-linear dependence on reference)
- ▶ Alternatives: fRMSE, signal/noise, correlation

## Conclusions (2/3)

How should we specify soil moisture observation errors for data assimilation?

- ▶ Specification of spatially uniform RMSE not sensible
- ▶ Use a uniform fRMSE, or even better spatial maps from triple collocation and error propagation (latter gives temporal variability)

## Conclusions (3/3)

Where should we focus future research on evaluating remotely sensed soil moisture?

- ▶ Given the available data, we can estimate errors in temporal behavior with reasonable confidence  
'No amount of statistical manipulation can add any new physical information on top of what already exists in the data products in use. A "real" better error assessment can only happen when new, better and independent data sources become available'. Pan et al, 2015.
- ▶ Other types of errors need more attention
  - ▶ Systematic errors (bias in mean, variance)
  - ▶ Errors in spatial patterns
- ▶ Data assimilation would benefit from realistic spatial error covariances